

Solution Set 1

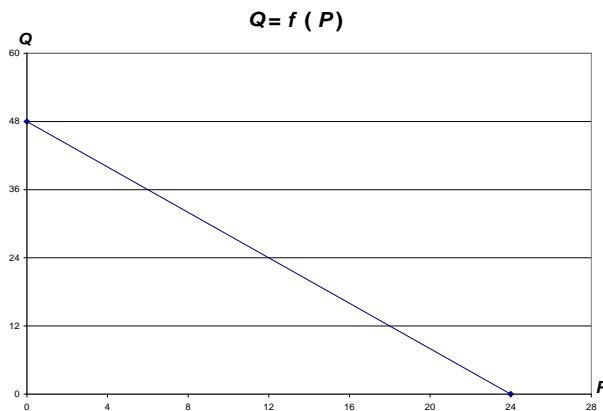
1. a) Choke price $Q = A - BP = 0$

$$BP = A$$

$$P = \frac{A}{B}$$

b) Plot $Q = 48 - 2P$

2 points $P = 0 \quad Q = 48$
 $Q = 0 \quad P = 24$



c) $P = f(Q)$

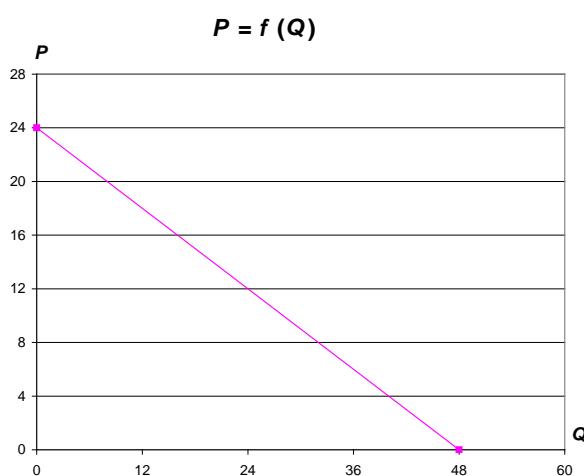
$$Q = A - BP$$

$$BP = A - Q$$

$$P = \frac{A}{B} - \frac{1}{B}Q$$

Plot $P = 24 - 0.5Q$

2 points $Q = 0 \quad P = 24$
 $P = 0 \quad Q = 48$



2. We are given $C = aH + bA$

We also know that

| Patient | Days in Hospital (H) | Hours of Attention (A) | Total Bill (C) |
|---------|----------------------|------------------------|----------------|
| 1 | 4 | 10 | \$500 |
| 2 | 7 | 30 | \$1125 |

Using the data on patient 1,

$$500 = 4a + 10b \Rightarrow a = \frac{500 - 10b}{4}$$

Using the data from patient 2,

$$7a + 30b = 1125$$

$$7\left(\frac{500 - 10b}{4}\right) + 30b = 1125 \quad \text{multiply both sides by 4}$$

$$4\left[7\left(\frac{500 - 10b}{4}\right) + 30b\right] = [1125]4$$

$$7(500 - 10b) + 120b = 4500$$

$$3500 - 70b + 120b = 4500$$

$$50b = 1000$$

$$b = 20$$

$$\text{Finally, } a = \frac{500 - 10b}{4} = \frac{500 - 10(20)}{4} = \frac{500 - 200}{4} = \frac{300}{4} = 75$$

$$C = 75H + 20A$$

3. We want to solve for P_w and P_b if $D_w = S_w$ and $D_b = S_b$.

$S_w = D_w$ gives

$$50 + 20P_w - 5P_b = 50 - 10P_w + 5P_b$$

$$30P_w = 10P_b$$

$$3P_w = P_b$$

$D_b = S_b$ gives

$$400 + 10P_w - 10P_b = -10P_w + 10P_b$$

$$400 = -20P_w + 20P_b$$

$$400 = -20P_w + 20(3P_w)$$

$$400 = -20P_w + 60P_w$$

$$400 = 40P_w$$

$$P_w = 10$$

$$P_b = 3P_w = 3(10) = 30$$

4. $P_d = -(Q + 4)^2 + 100 = -(Q^2 + 8Q + 16) + 100$

$$P_d = -Q^2 - 8Q + 84$$

$$P_s = (Q + 2)^2 = Q^2 + 4Q + 4$$

Equilibrium when $P_d = P_s$

$$-Q^2 - 8Q + 84 = Q^2 + 4Q + 4$$

$$2Q^2 + 12Q - 80 = 0$$

$$Q^2 + 6Q - 40 = 0$$

$$a = 1$$

$$b = 6$$

$$c = -40$$

$$Q = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} = \frac{-6 \pm \sqrt{36 + 4*40}}{2} = \frac{-6 \pm \sqrt{196}}{2}$$

$$Q_1 = \frac{-6 + 14}{2} = 4 \quad Q_2 = \frac{-6 - 14}{2} = -10 \text{ impossible}$$

Market equilibrium for $Q = 4$

$$P = (Q + 2)^2 = 6^2 = 36$$

5. Price = f (demand) Express demand in hundreds

$$P = a + bD$$

$$140 = a + b*3$$

$$92 = a + b*11$$

Substract (2) from (1)

$$48 = -8b$$

$$b = -\frac{48}{8} = -6$$

replace b by -6 in (1)

$$140 = a + (-6) * 3 = a - 18$$

$$a = 140 + 18 = 158$$

$$P = 158 - 6D$$

Price at a demand of 700 watches?

$$P = f(7) = 158 - 6 * 7 = 158 - 42 = 116$$

Price at a demand of 1200 watches

$$P = f(12) = 158 - 6 * 12 = 158 - 72 = 86$$

6. Let $x = \#$ of magazine units, and $y = \#$ of television units.
 Budget = (a) ($\#$ magazine units) + (c) ($\#$ television units), or
 $B = ax + cy$.

Recall the manager wants to buy twice as many television units as magazine units,
 i.e. wants $y = 2x$. Substituting,

$$\begin{aligned} B &= ax + c(2x) \\ &= x(a + 2c) \end{aligned}$$

$$x = \frac{B}{a + 2c}$$

7.

| x | y |
|---------------------------|-------------------------------------|
| Activity level (units) | Total Production Cost (‘000s) |
| 5000 | 100 |
| 40000 | 240 |

Linear equations can be written in the form $y = mx + b$

$$m = \text{slope} = \frac{y_2 - y_1}{x_2 - x_1} = \frac{240\ 000 - 100\ 000}{40\ 000 - 5\ 000} = \frac{140\ 000}{35\ 000} = 4, \text{ so}$$

$$y = 4x + b$$

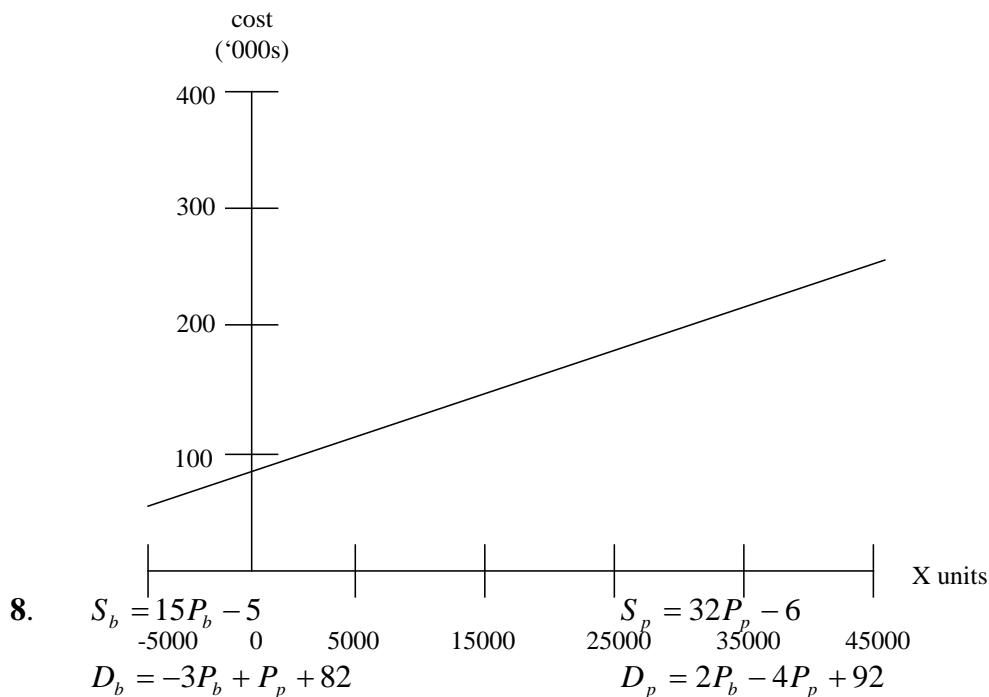
b = y intercept = total cost when activity level = 0.

To find b , plug in known values for x and y and solve for b :

$$b = y - 4x = 100\ 000 - 4(5\ 000) = 80\ 000,$$

in other words, fixed cost = \$ 80 000

The equation of the line is $y = 4x + 80\ 000$, the corresponding graph is shown below



8.

$$S_b = 15P_b - 5$$

$$D_b = -3P_b + P_p + 82$$

$$S_b = D_b$$

$$15P_b - 5 = -3P_b + P_p + 82$$

$$18P_b - P_p = 87$$

$$P_p = 18P_b - 87$$

$$36(18P_b - 87) - 2P_b = 98$$

$$648P_b - 3132 - 2P_b = 98$$

$$646P_b = 3230$$

$$P_b = 5$$

$$P_p = 18(5) - 87 = 3$$

$$D_b = S_b = 15(5) - 5 = 70$$

$$D_p = S_p = 32(3) - 6 = 90$$

9. Demand function:

$$P = 1000 \quad Q = 10$$

$$P = 2000 \quad Q = 6$$

P is a linear function of Q

$$P = a + bQ$$

$$1000 = a + b * 10$$

$$2000 = a + b * 6$$

Subtract the first equation from the second

$$1000 = -4b$$

$$b = -\frac{1000}{4} = -250$$

$$a = 2000 - 6b = 2000 - 6 * (-250)$$

$$a = 2000 + 1500$$

$$a = 3500$$

Demand function $P = 3500 - 250Q$

Supply function $P = 500 + 125Q$

Market equilibrium: Supply = Demand

$$500 + 125Q = 3500 - 250Q$$

$$125Q + 250Q = 3500 - 500$$

$$375Q = 3000$$

$$Q = \frac{3000}{375} = 8$$

$$P = 500 + 125 * 8 = 1500$$

10. Let's use demand in thousands:

1. Price = f (demand)

$$P = 88 \quad D = 2$$

$$P = 38 \quad D = 12$$

$$P = a + bD$$

$$88 = a + b * 2$$

$$38 = a + b * 12$$

From the first equation

$$a = 88 - 2b$$

Report in the second equation

$$38 = 88 - 2b + 12b$$

$$38 - 88 = 10b$$

$$\frac{-50}{10} = b$$

$$-5 = b$$

$$a = 88 - 2b = 88 - 2 * (-5) = 98$$

So the price function is

$$P = 98 - 5D$$

$$\text{If } D = 8, \quad P(8) = 98 - 5 * 8 = 58$$

$$\text{If } D = 15, \quad P(15) = 98 - 5 * 15 = 23$$

2. Demand = f (price)

$$D = 2 \quad P = 88$$

$$D = 12 \quad P = 38$$

$$D = a + bP$$

$$2 = a + b * 88$$

$$12 = a + b * 38$$

$$a = 2 - 88b$$

$$12 = 2 - 88b + 38b$$

$$12 - 2 = -50b$$

$$\frac{-10}{50} = b$$

$$-0.2 = b$$

$$a = 2 - 88b = 2 - 88 * (-0.2) = 2 + 17.6$$

$$a = 19.6$$

$$D = 19.6 - 0.2P$$

$$\text{If } D = 8, \quad 8 = 19.6 - 0.2P$$

$$0.2P = 11.6$$

$$P = \frac{11.6}{0.2} = 58$$

If $D = 15$, $15 = 19.6 - 0.2P$

$$0.2P = 4.6$$

$$P = \frac{4.6}{0.2} = 23$$